

# Neutrino oscillation physics

08 October 2020

**ESSnuSB Workshop**  
**UHH - Barenfeld - DESY**

**Silvia Pascoli**

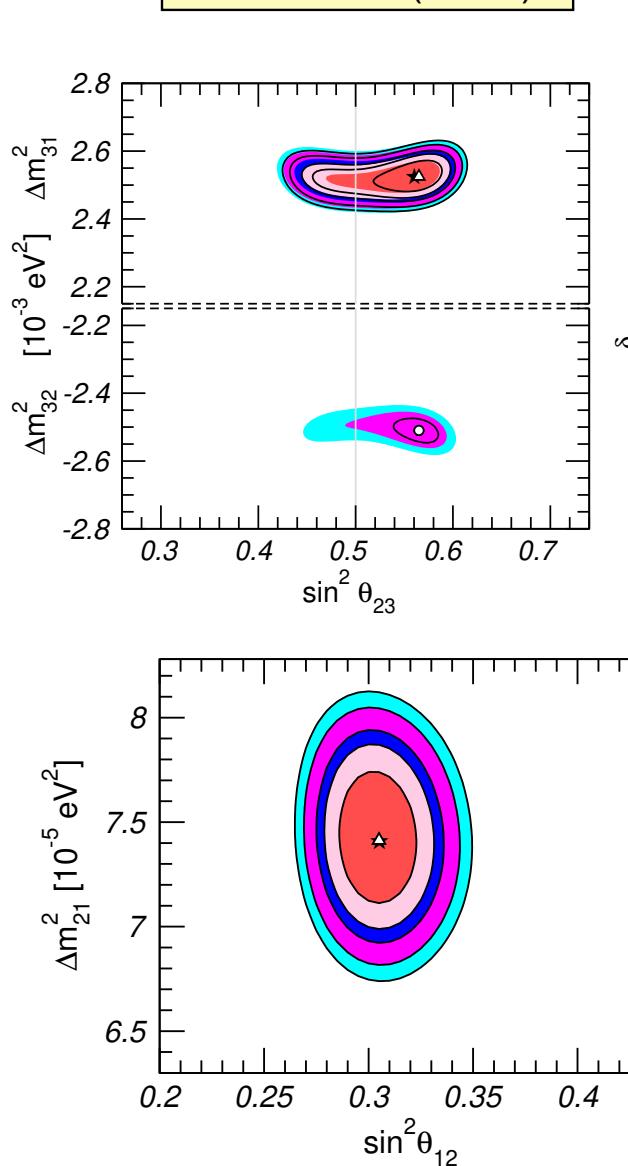
**IPPP – Durham University**

T2K event



# Neutrino properties after July 2019

NuFIT 4.1 (2019)

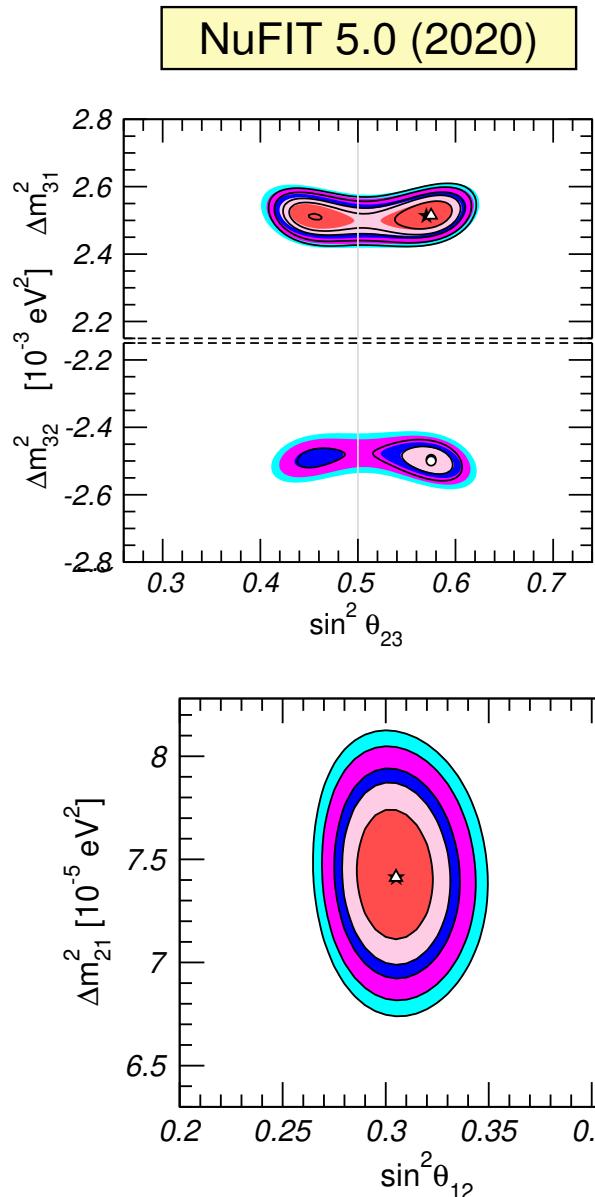


Neutrinos have masses and mix!

Current knowledge of neutrino properties:

- 2 mass squared differences
- 3 sizable mixing angles,
- hints of CPV
- indications in favour of NO

# Neutrino properties after July 2020



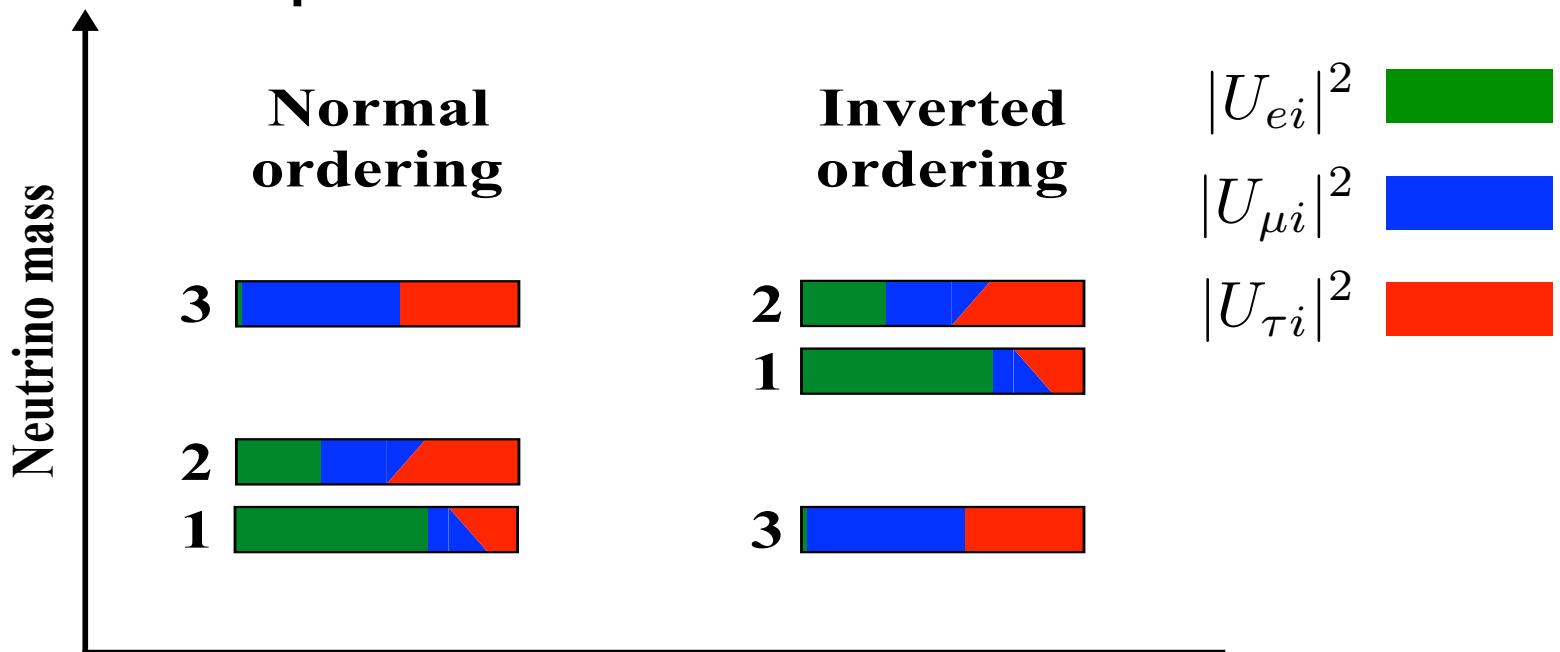
Neutrinos have masses and mix!

Current knowledge of neutrino properties:

- 2 mass squared differences
- 3 sizable mixing angles,
- some hints of CPV
- preference for NO

# Neutrino masses

$\Delta m_{21}^2 \ll \Delta m_{31}^2$  implies at least 3 massive neutrinos.



Fractional flavour content of massive neutrinos

$$m_1 = m_{\min}$$

$$m_2 = \sqrt{m_{\min} + \Delta m_{21}^2}$$

$$m_3 = \sqrt{m_{\min} + \Delta m_{31}^2}$$

$$m_3 = m_{\min}$$

$$m_1 = \sqrt{m_{\min} + |\Delta m_{32}^2| - \Delta m_{21}^2}$$

$$m_2 = \sqrt{m_{\min} + |\Delta m_{32}^2|}$$

Measuring the masses requires:

- the mass scale:  $m_{\min}$
- the MO: mild preference for NO ( $\Delta\chi^2 \sim 2.7(1.6\sigma)$ ).

# Leptonic Mixing and CP-violation

## The Pontecorvo-Maki-Nakagawa-Sakata matrix

$$\nu_i = U^\dagger \nu_\alpha \longrightarrow \mathcal{L}_{CC} = \frac{g}{\sqrt{2}} (\bar{e}_L, \bar{\mu}_L, \bar{\tau}_L) \gamma^\mu \mathbf{U}_{\text{osc}} \begin{pmatrix} \nu_{1L} \\ \nu_{2L} \\ \nu_{3L} \end{pmatrix} W_\mu$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \\ c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13} e^{-i\delta} & 0 & c_{13} \\ 1 & 0 & 0 \\ 0 & e^{i\alpha_{21}/2} & 0 \\ 0 & 0 & e^{i\alpha_{31}/2} \end{pmatrix}$$

CPV?

- Mixings very different from quark sector.
- Possibly, large leptonic CPV.  
CPV is a fundamental question, possibly related to the origin of the baryon asymmetry and to the origin of the flavour structure.

# *Phenomenology questions for the future*

- 1. What is the nature of neutrinos?**
- 2. What are the values of the masses? Absolute scale and the ordering.**
- 3. Is there leptonic CP-violation?**
- 4. What are the precise values of mixing parameters?**
- 5. Is the standard picture correct? Are there NSI? Sterile neutrinos? Other effects?**

**Very exciting experimental programme now and for the future.**

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**Long baseline  
neutrino  
oscillation  
experiments**

**Very exciting experimental programme now  
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# Neutrino oscillations

Let's assume that at  $t=0$  a muon neutrino is produced

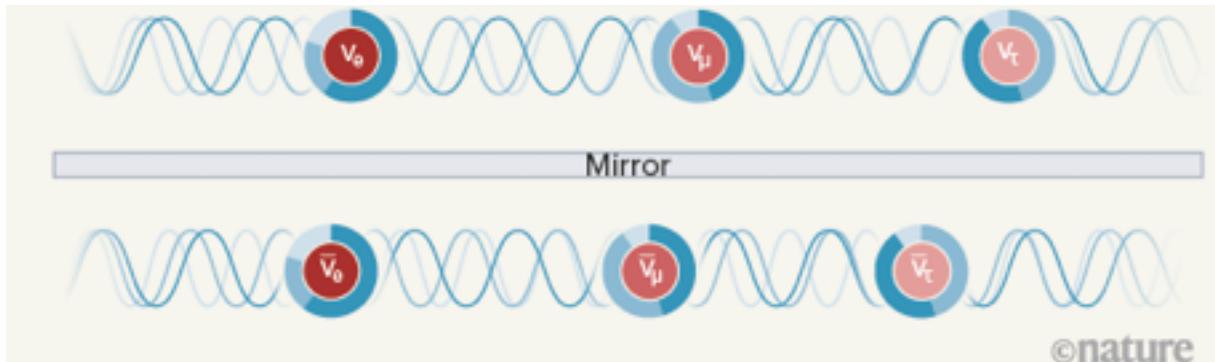
$$|\nu, t = 0\rangle = |\nu_\mu\rangle = \sum_i U_{\mu i} |\nu_i\rangle$$

The time-evolution is given by the solution of the Schroedinger equation with free Hamiltonian:

$$|\nu, t\rangle = \sum_i U_{\mu i} e^{-i E_i t} |\nu_i\rangle$$

At detection, projecting over the flavour state :

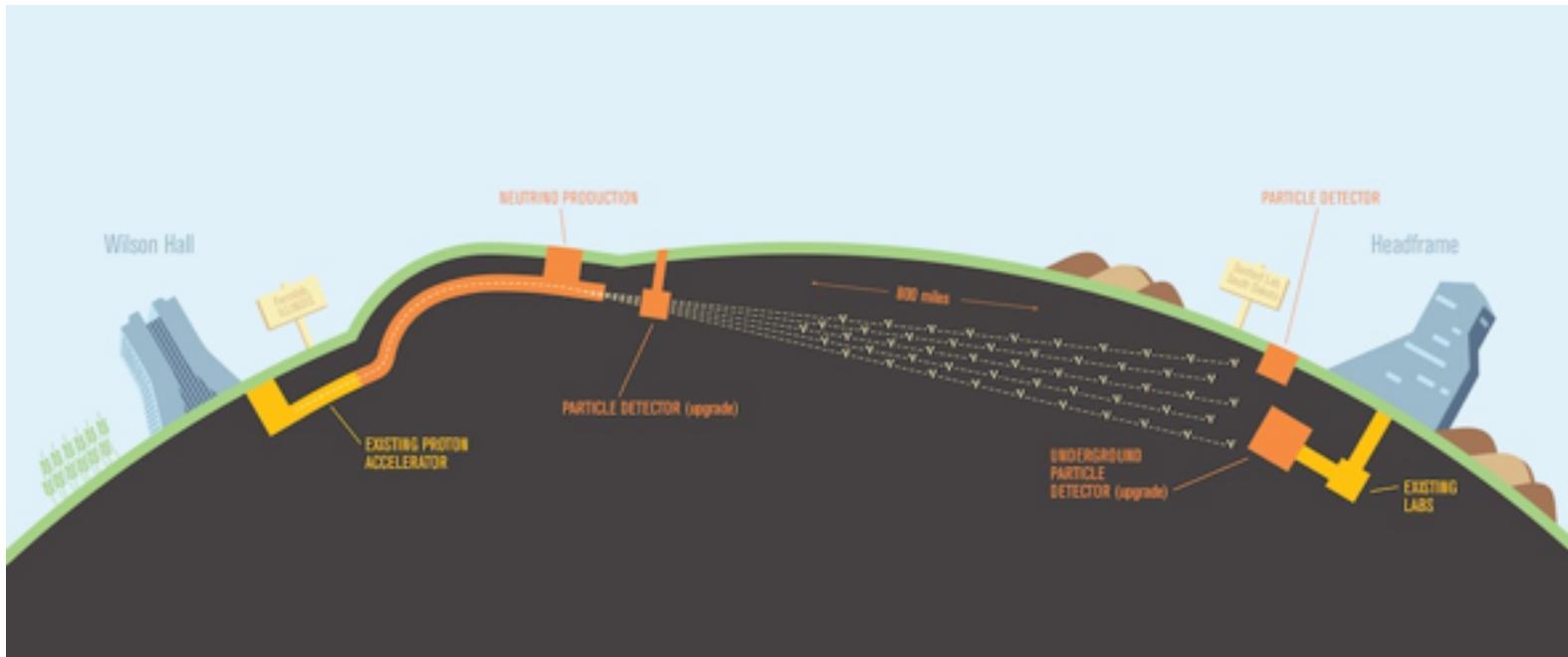
$$P(\nu_\alpha \rightarrow \nu_\beta) = \left| \sum_i U_{\alpha 1} U_{\beta 1}^* e^{-i \frac{\Delta m_{i1}^2}{2E} L} \right|^2 = \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E_\nu}$$



Nature, SP and J.  
Turner, News and  
views, 15 April 2020

# **Long-baseline neutrino oscillations and the mass ordering**

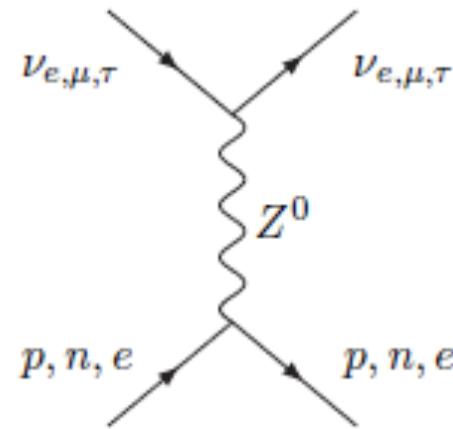
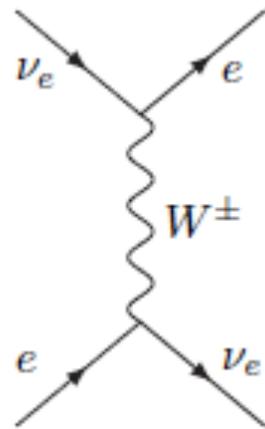
- When neutrinos travel through a medium, they interact with the background of e, p and n.



Credit:  
Symmetry  
magazine

- The background is CP and CPT violating, e.g. the Earth contains only particle and not antiparticles, and the resulting oscillations are CP and CPT violating.

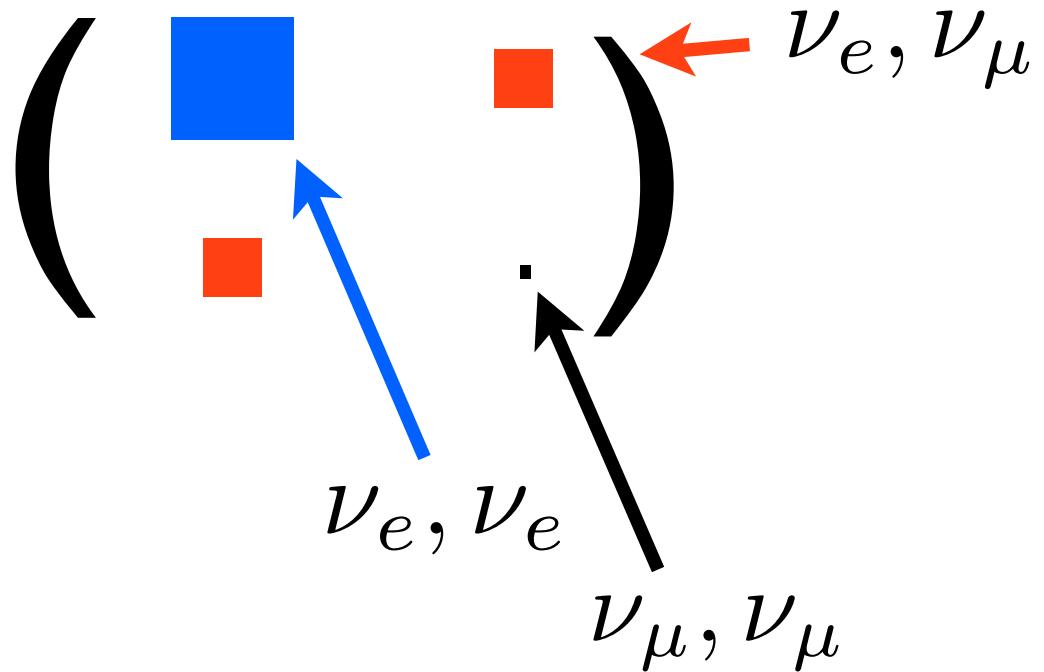
- Neutrinos undergo forward elastic scattering via CC and NC interactions.



- Matter effects are described by a potential  $V$  in the effective Hamiltonian which determines the time evolution.

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} -\frac{\Delta m^2}{4E} \cos(2\theta) + \sqrt{2}G_F N_e & \frac{\Delta m^2}{4E} \sin(2\theta) \\ \frac{\Delta m^2}{4E} \sin(2\theta) & \frac{\Delta m^2}{4E} \cos(2\theta) \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

## Effective Hamiltonian in the flavour basis



## Effective Hamiltonian

$$\begin{pmatrix} \text{blue square} & & \\ & \text{red square} & \\ & & \ddots \end{pmatrix}$$

$$\begin{pmatrix} \text{green square} & & \\ & \text{red square} & \\ & & \ddots \end{pmatrix}$$

$$\begin{pmatrix} \text{blue square} & & \\ & \text{red square} & \\ & & \ddots \end{pmatrix}$$

## Mixing angle

vacuum

$$\tan 2\theta \sim \frac{2 \text{ red square}}{\text{blue square}}$$

matter suppression (Sun, SN)

$$\tan 2\theta^M \sim \frac{2 \text{ red square}}{\text{blue square} + \text{green square}} \ll \tan 2\theta$$

MSW resonance (Sun, SN)

$$\tan 2\theta^M \sim \frac{2 \text{ red square}}{\text{blue square} - \text{white square}} \sim \infty$$

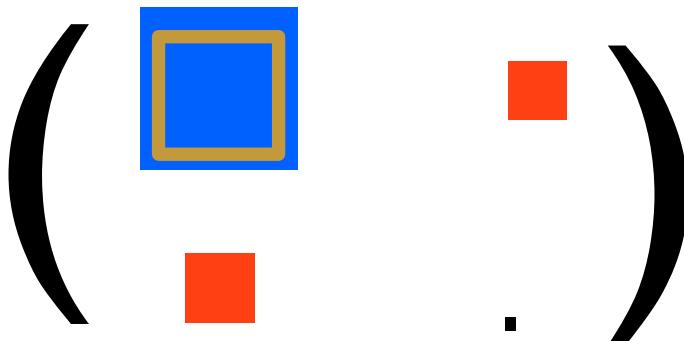
## In long baseline experiments

$$-\frac{\Delta m^2}{2E} \cos(2\theta)$$

$$\nu + \sqrt{2}G_F N_e$$

$$\bar{\nu} - \sqrt{2}G_F N_e$$

For neutrinos

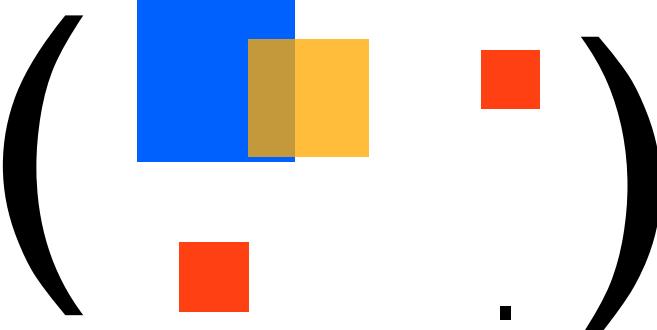


$$\Delta m^2 > 0$$

enhancement

$$\tan 2\theta^M \sim \frac{2 \textcolor{red}{\square}}{\textcolor{blue}{-} + \textcolor{orange}{+}}$$

For antineutrinos



$$\Delta m^2 > 0$$

suppression

$$\tan 2\theta^M \sim \frac{2 \textcolor{red}{\square}}{\textcolor{blue}{-} + \textcolor{orange}{-}}$$

# The 3 neutrino probability can be approximated as

$$P_{\mu e} \simeq 4c_{23}^2 s_{13}^2 \frac{1}{(1 - r_A)^2} \sin^2 \frac{(1 - r_A)\Delta_{31}L}{4E}$$

A. Cervera et al., hep-ph/0002108;  
 K. Asano, H. Minakata, 1103.4387;  
 S. K. Agarwalla et al., 1302.6773;  
 P. Denton, S. Parke and X. Zhang,  
 1907.02534...

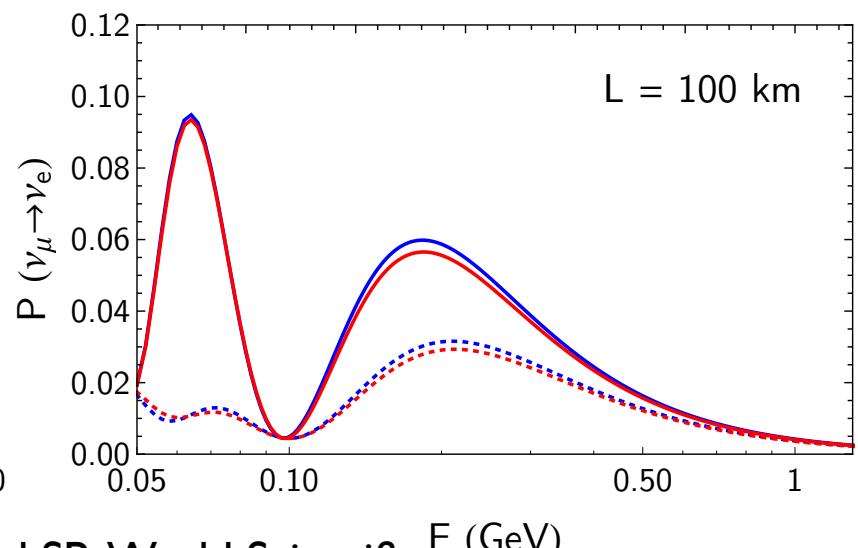
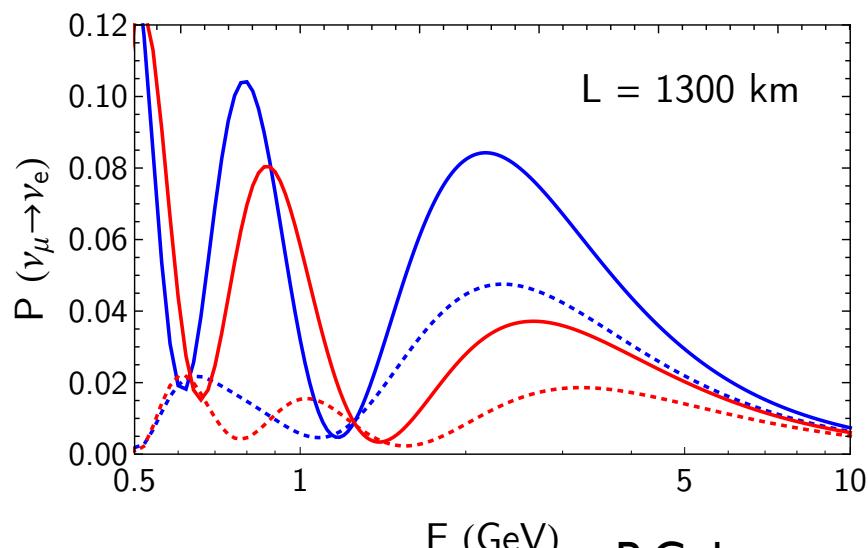
$$+ \sin 2\theta_{12} \sin 2\theta_{23} s_{13} \frac{\Delta_{21}L}{2E} \sin \frac{(1 - r_A)\Delta_{31}L}{4E} \cos \left( \delta - \frac{\Delta_{31}L}{4E} \right)$$

$$+ s_{23}^2 \sin^2 2\theta_{12} \frac{\Delta_{21}^2 L^2}{16E^2} - 4c_{23}^2 s_{13}^4 \sin^2 \frac{(1 - r_A)\Delta_{31}L}{4E}$$

with

$$\Delta_{31} \equiv \Delta m_{31}^2 / (2E_\nu)$$

$$r_A \simeq \frac{\sqrt{2}G_F N_e}{\Delta m_{31}^2 / (2E_\nu)}$$



# Long-baseline neutrino oscillations and leptonic CP violation

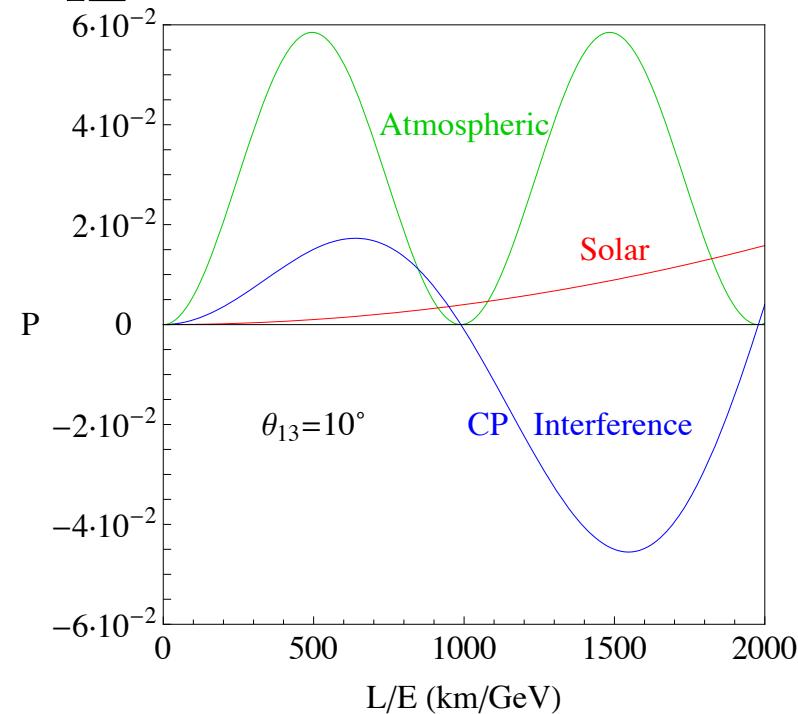
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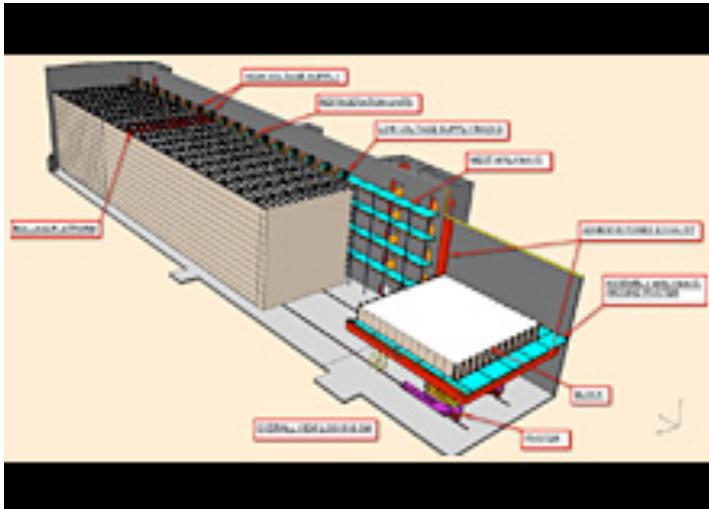
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A. Cervera et al., hep-ph/0002108;  
 K. Asano, H. Minakata, 1103.4387;  
 S. K. Agarwalla et al., 1302.6773...

- The determination of CPV and of the mass ordering are entangled.
- Matter effects increase with energy and distance.
- CPV effects more pronounced at low energy.

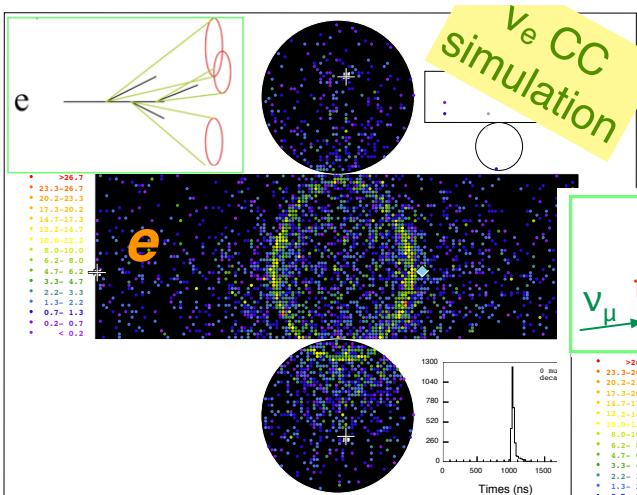


# Present/Future LBL exp DUNE: 1300 km

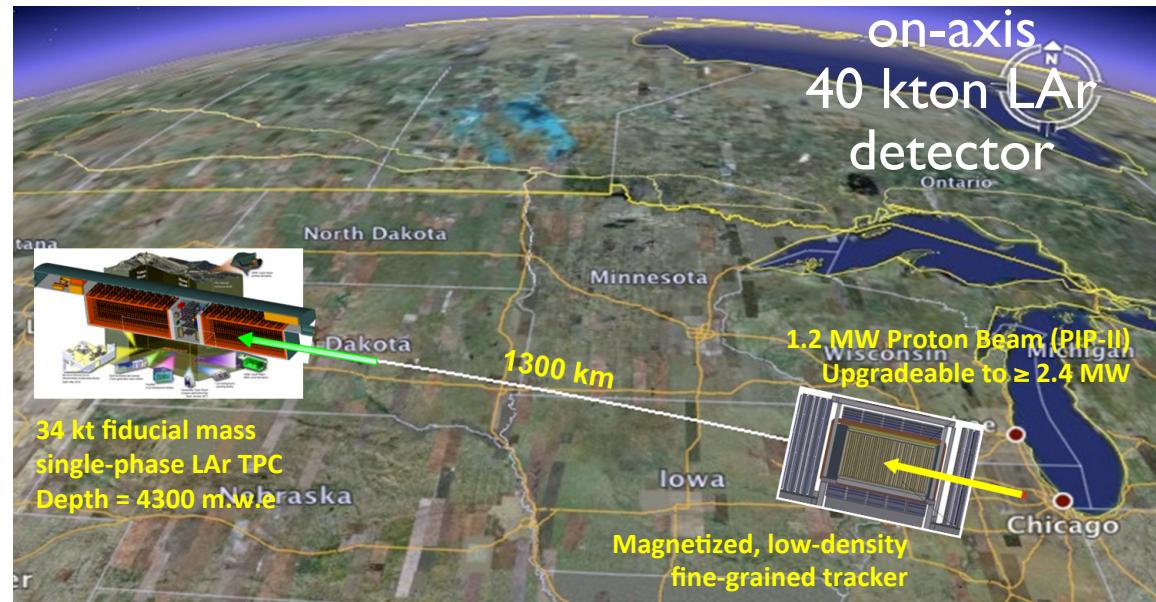


**NOvA:** 810 km off-axis  
~14 kton plastic scintillator detector

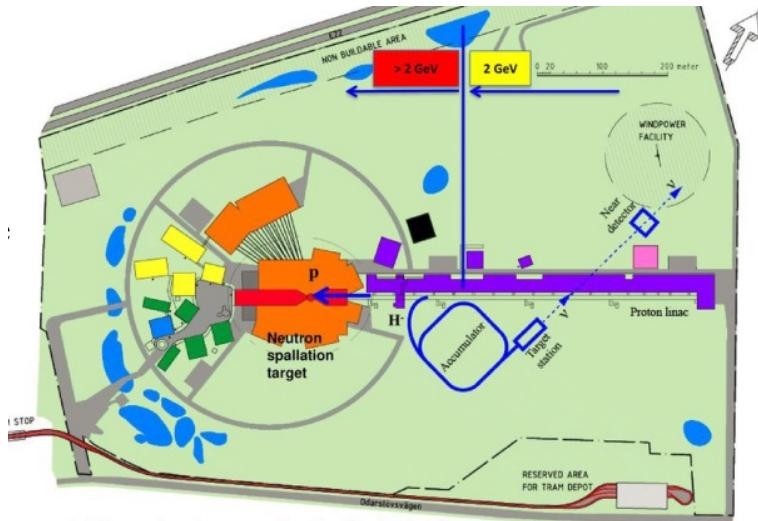
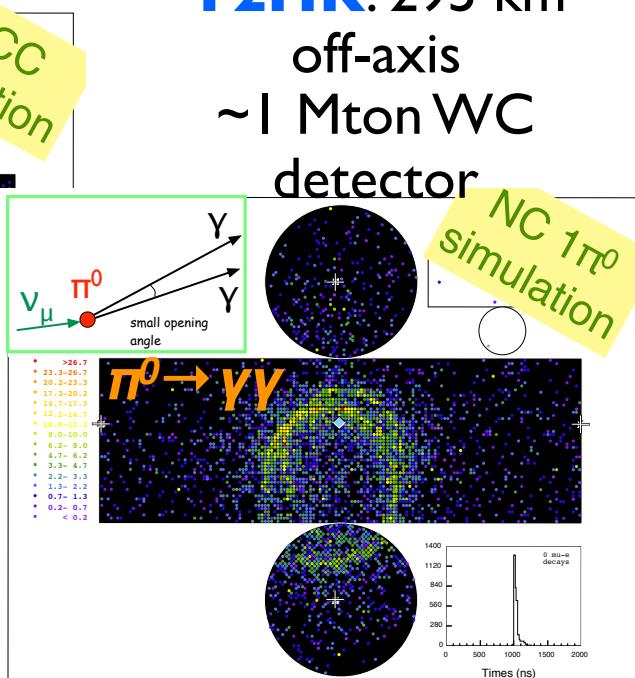
**T2K:** 295 km off-axis  
~22.5 kton WC detector



M. Shiozawa, for  
T2HK coll., NuPhys  
2014



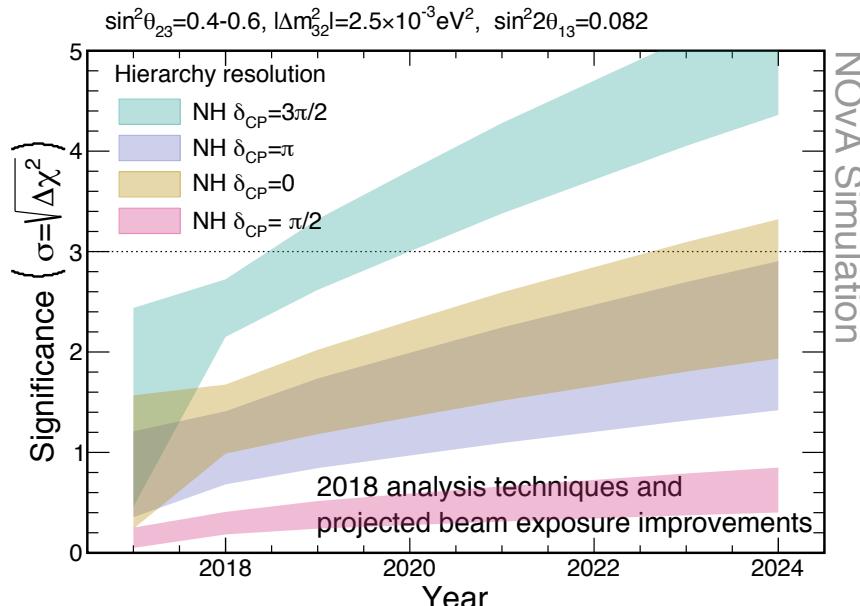
**T2HK:** 295 km  
off-axis  
~1 Mton WC  
detector



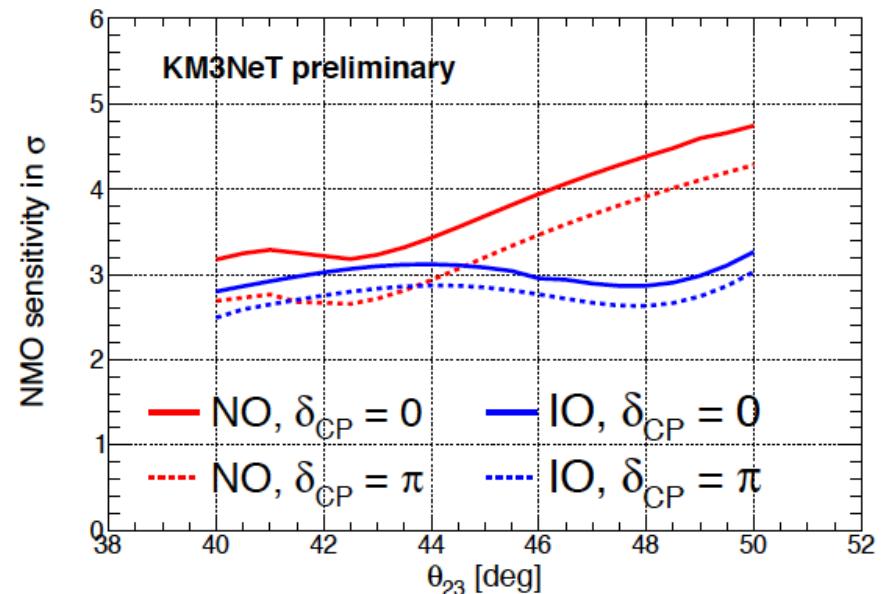
~1 BEuros for the neutrino facility including detector

**ESSnuSB:** 300-500 km  
~0.5 Mton WC detector  
second osc. maximum

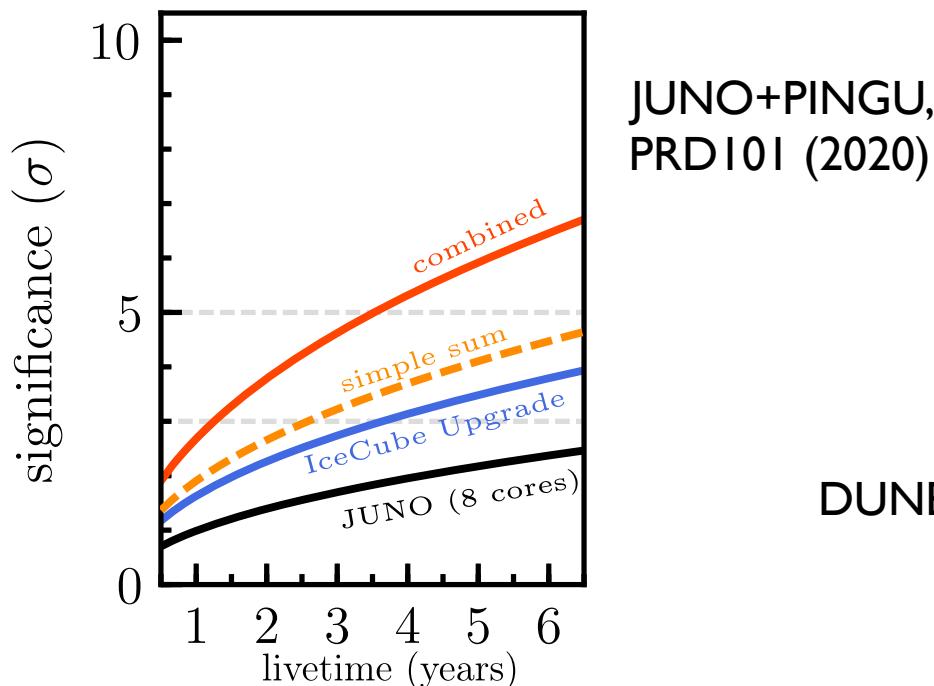
# Mass ordering sensitivity



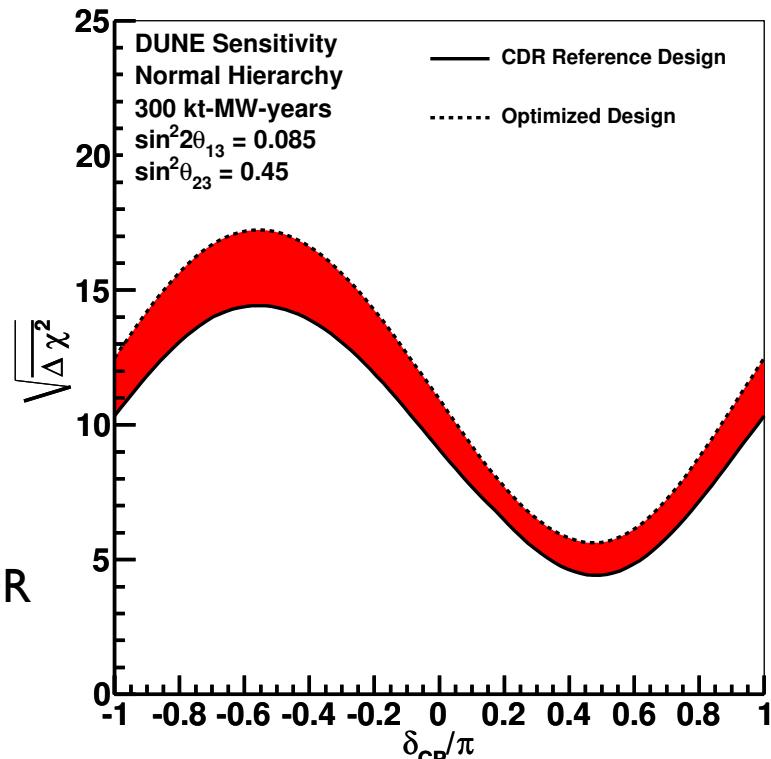
M. Sanchez, Neutrino 2018



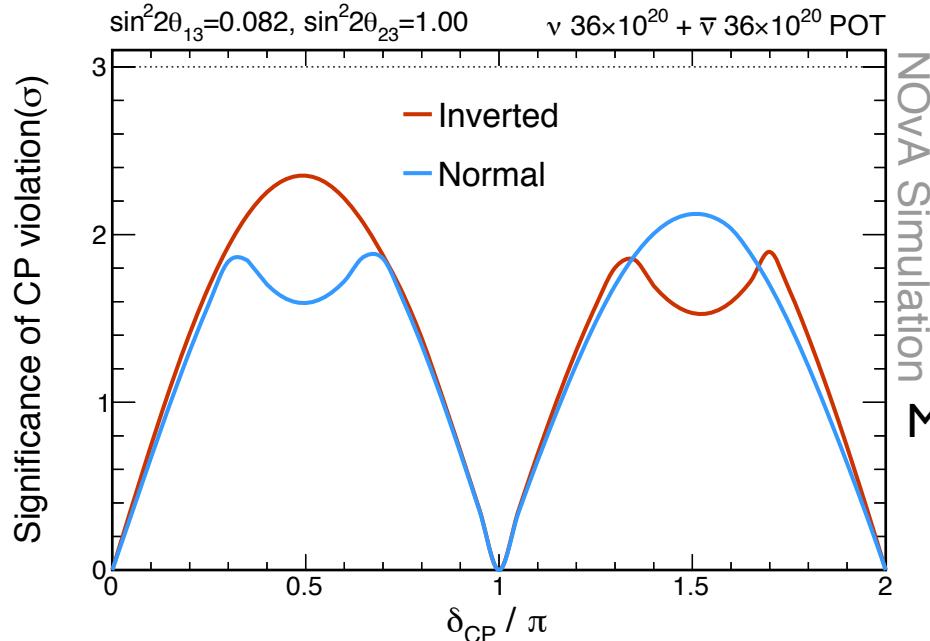
KM3Net, ORCA Coll., 2004.05004



DUNE CDR

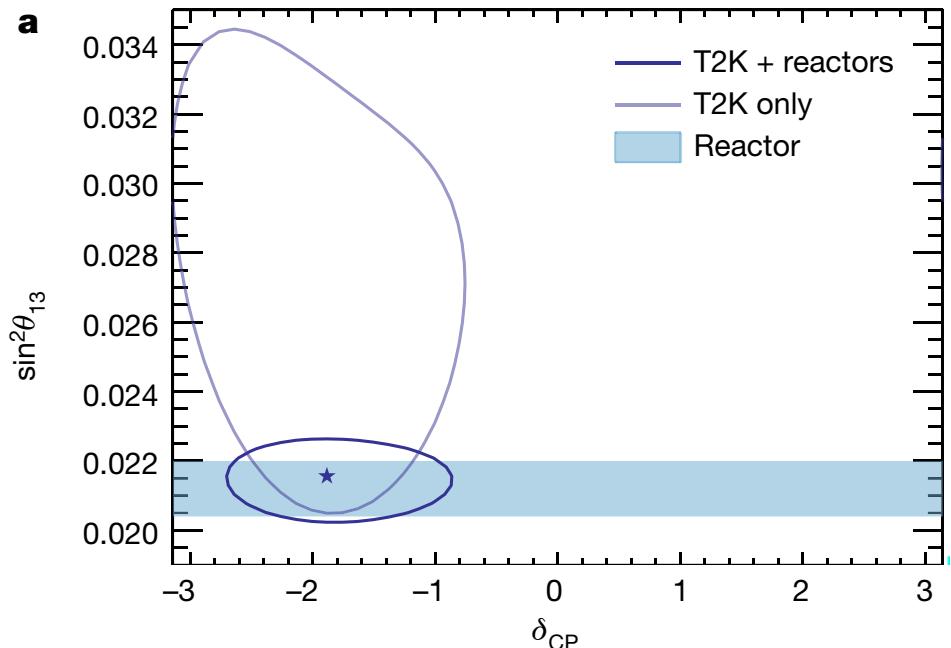


# CPV sensitivity



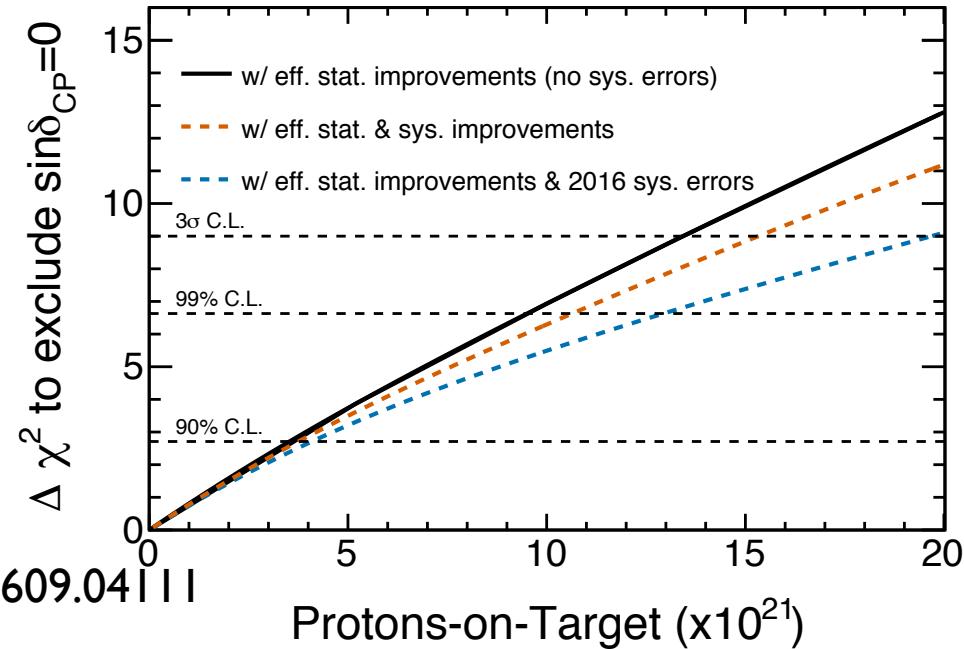
NOvA plans an extended run till 2024 (50% nu, 50% antinu) with further accelerator improvements.

M. Sanchez, Neutrino 2018



T2K Coll., Nature 580 (2020)

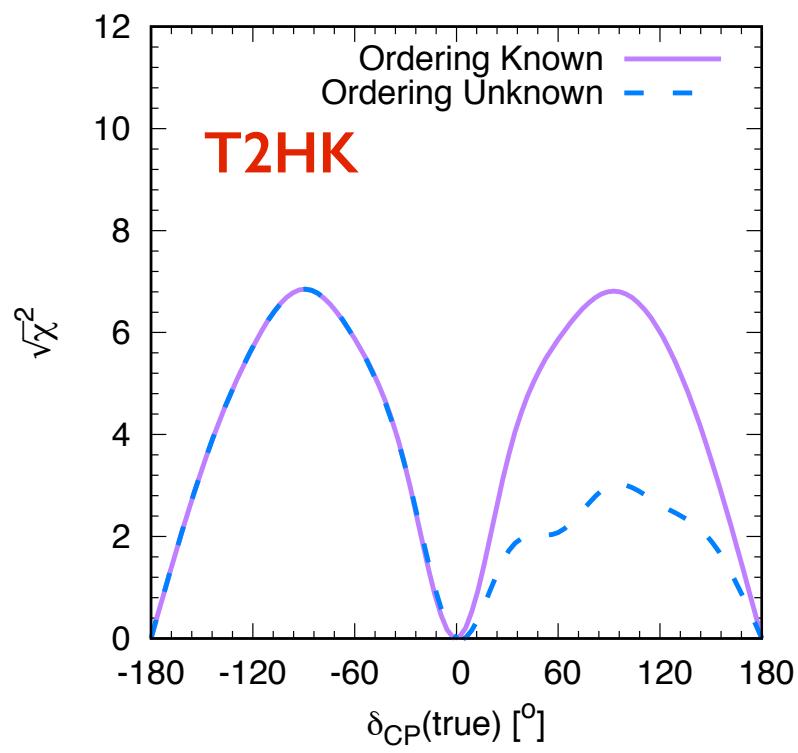
T2K phase 2 extension aims at reaching 1.3 MW by 2026 (20 $\times 10^{21}$  pot).



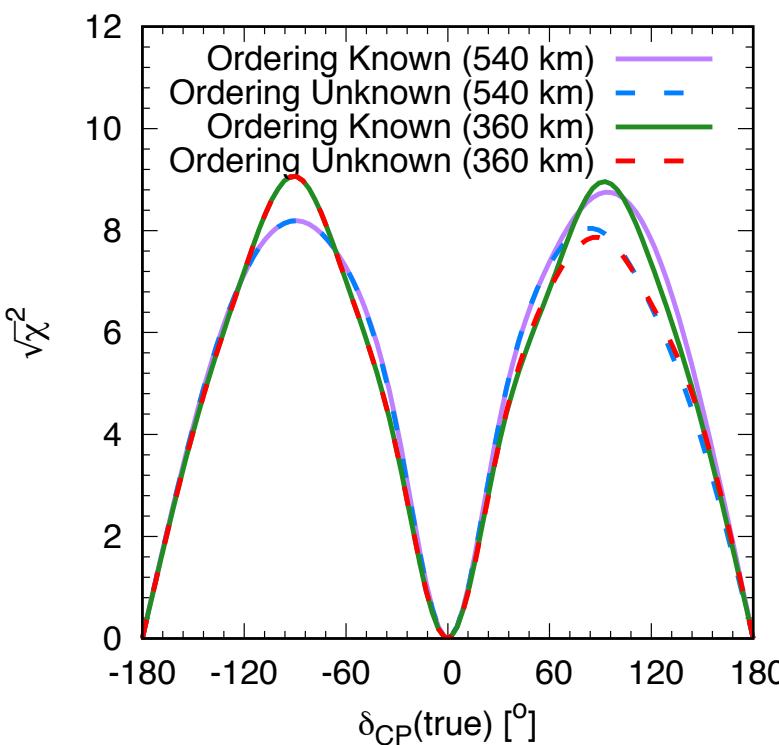
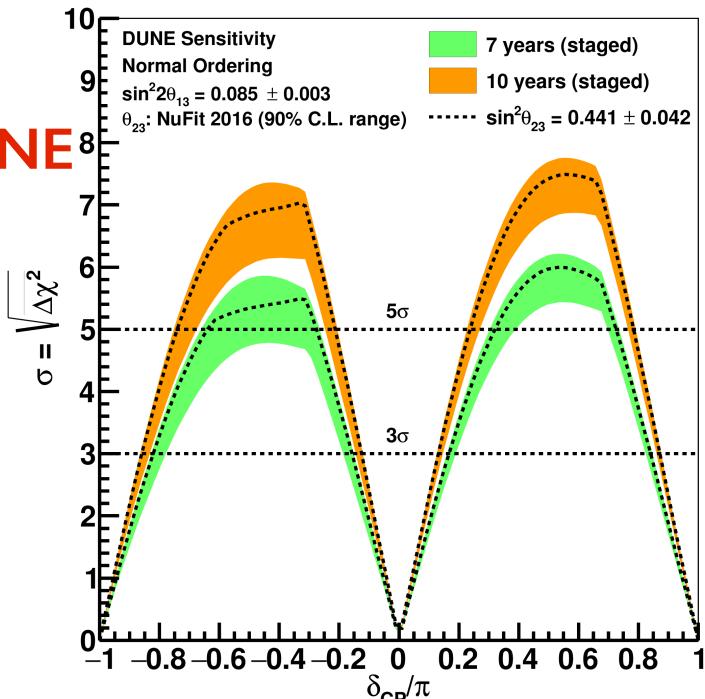
T2K, 1609.04111



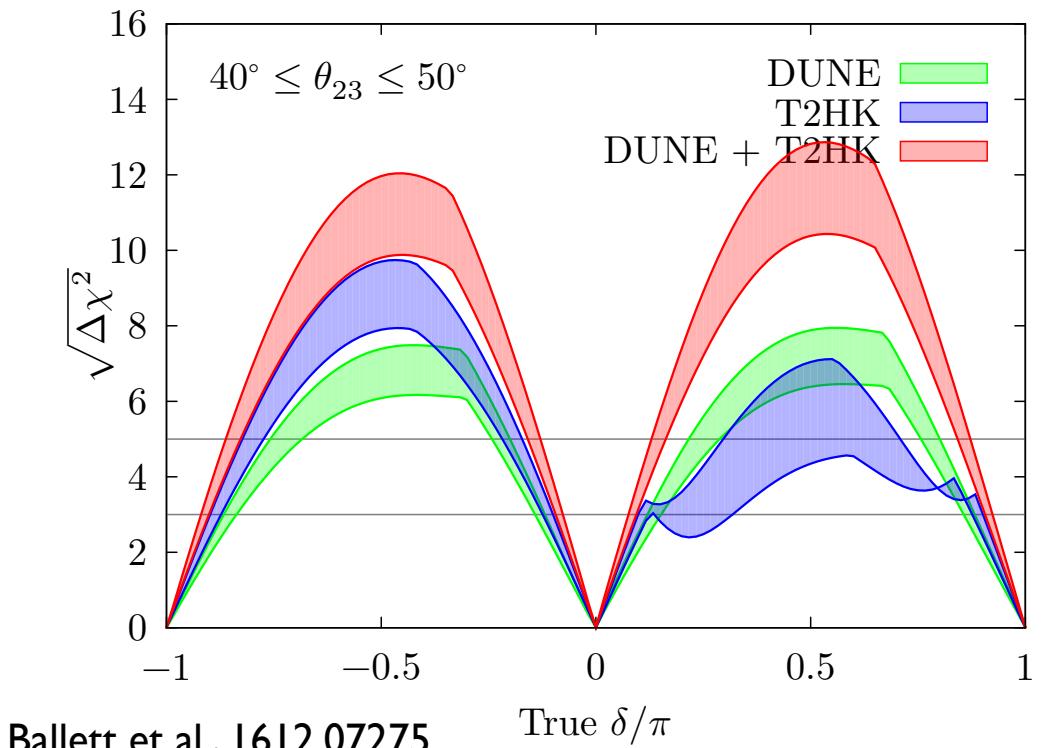
T2HK



ESSnuSB

**DUNE**

E.Worcester, for DUNE, Neutrino 2018



Ballett et al., 1612.07275

True  $\delta/\pi$

# Precision measurements of the oscillation parameters in LBL experiments

The precision measurement of the oscillation parameters is a primary physics goal for LBL experiments.

- The values of the mixing angles seem to indicate an underlying symmetry:  $\theta_{23} \sim 45^\circ$ ,  $\theta_{13}$  not too far from 0.
- Predictions for the CPV phase delta and relations among parameters in flavour models (e.g. sum rules), e.g.:

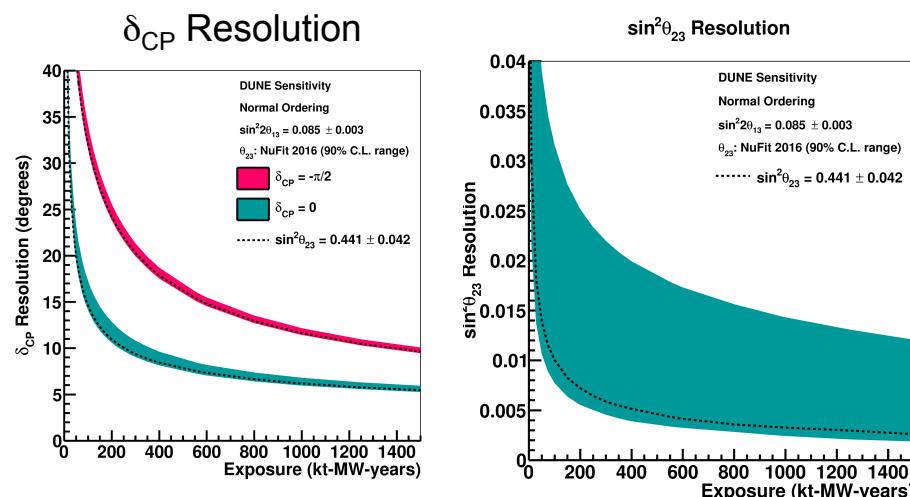
$$a = \sigma r \cos \delta \quad \sigma = 1, -1/2$$

with  $\sin \theta_{12} = \frac{1+s}{\sqrt{3}}$ ,  $\sin \theta_{13} = \frac{r}{\sqrt{2}}$ ,  $\sin \theta_{23} = \frac{1+a}{\sqrt{2}}$

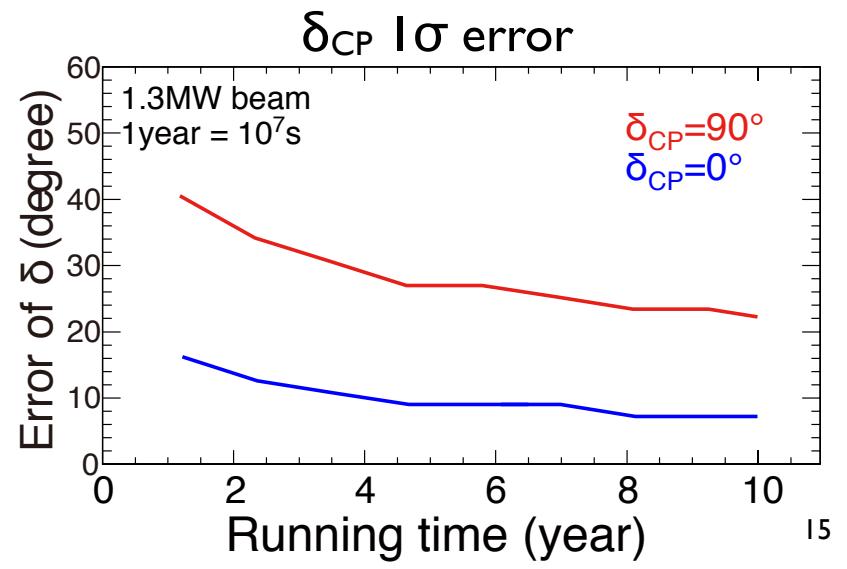
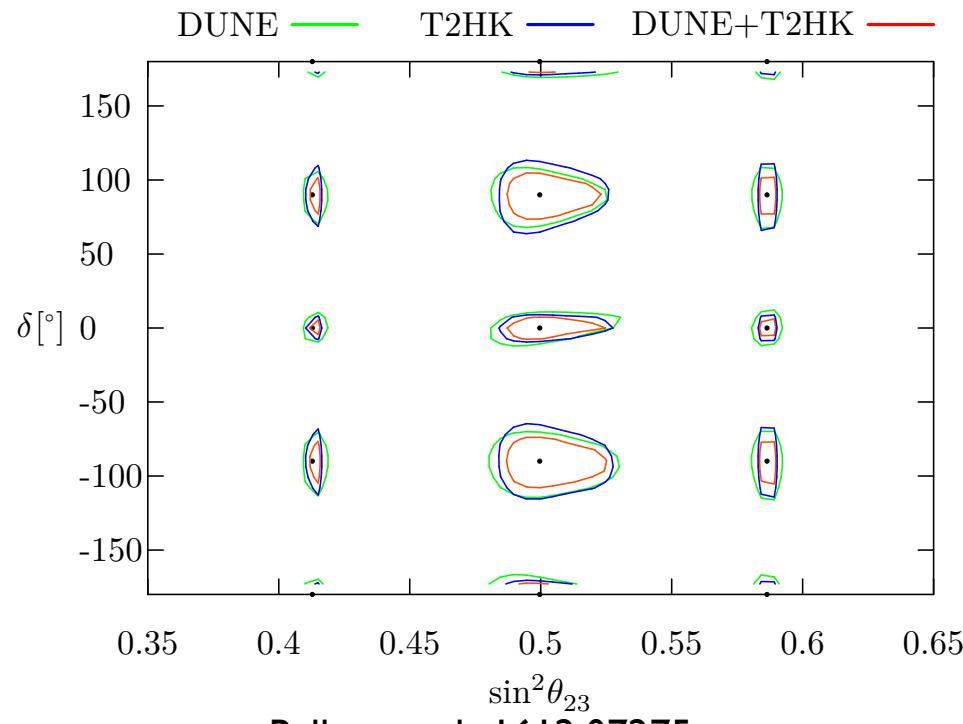
King, 0710.0530

Crucial information in order to discriminate between different flavour models.

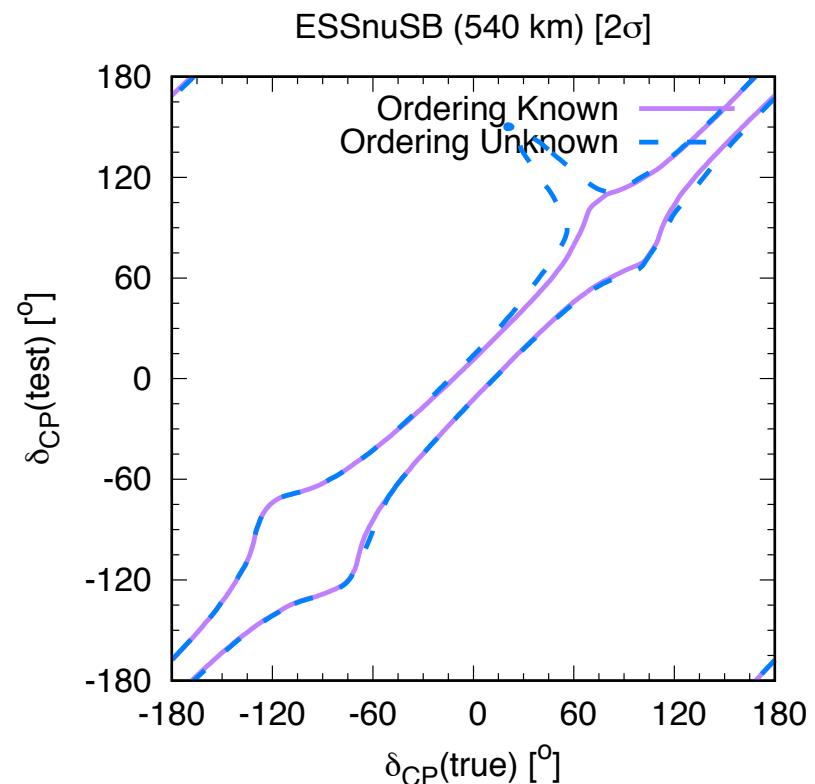
DUNE CDR:



E.Worcester, for DUNE, Neutrino 2018



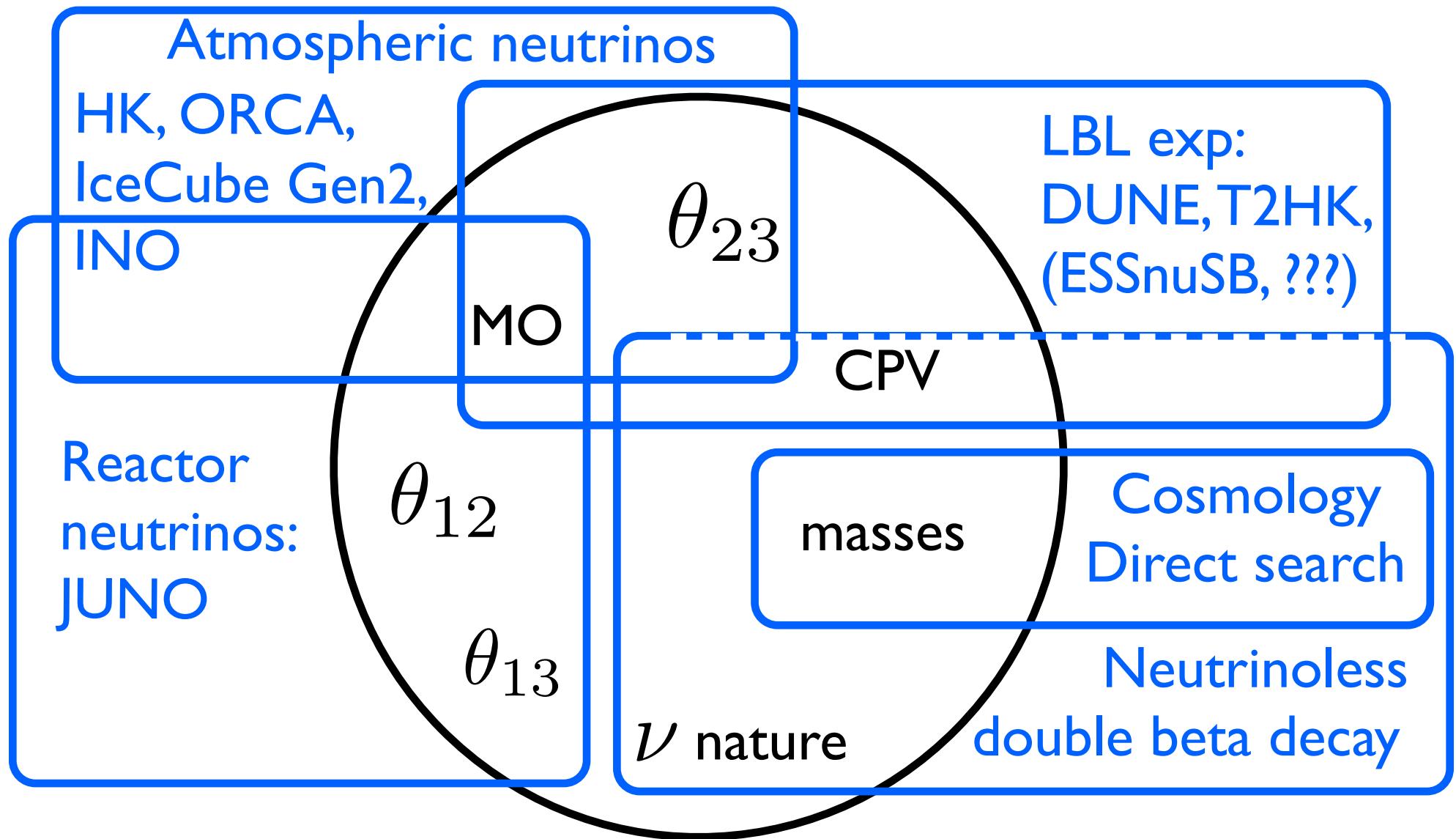
M. Shiozawa, for HK, Neutrino 2018



M. Ghosh and T. Ohlsson, 1906.05779

# Complementarity with other experiments

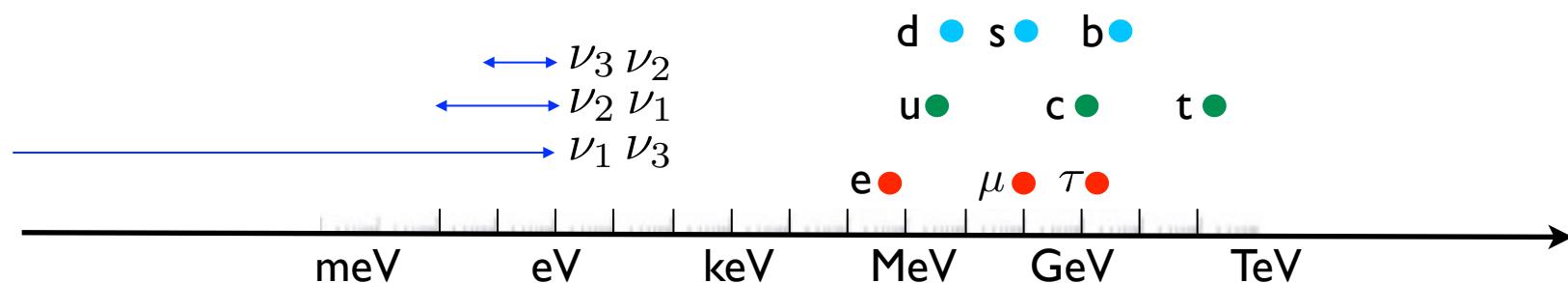
|                | 2020  | 2025              | 2030   | 2035                                       |
|----------------|---|-------------------|--|--|
| LBL<br>osc.    | <b>T2K</b><br><b>NOvA</b>                                 |                   | <b>LBNF-DUNE</b><br><b>T2HK (T2HKK)</b>                          | <b>ESSnuSB,</b><br><b>nufactory?</b>       |
| SBL<br>osc.    | <b>SBL reactor,...</b><br><b>MicroBooNE</b><br><b>SBN</b> |                   | <b>LBNF-DUNE ND</b><br><b>T2HK ND</b><br>???                     |  |
| Other<br>osc.  | <b>SK, Borexino,</b><br><b>LBL detectors</b>              |                   | <b>DUNE</b><br><b>HK</b>   | <b>Theia???</b>                            |
| Direct<br>mass |   | <b>JUNO</b>       |  |  |
| DBD0<br>nu     | <b>KATRIN</b>   |                   | <b>Project 8</b>   |  |
| UHE            | <b>KamLAND-Zen</b><br><b>GERDA, CUORE</b>                 | <b>LEGEND-200</b> | <b>LEGEND-1000</b><br><b>CUPID, NEXT-HD,</b><br><b>PANDAX...</b> | <b>Next</b><br><b>-next</b><br><b>gen?</b> |
|                | <b>IceCube</b>  |                   | <b>IceCubeGen2</b><br><b>ORCA, KM3Net</b>                        |  |



Tests of standard neutrino paradigm: SBL oscillations (SBN, reactor exp), LBL/atm oscillations, neutrino less DBD, beta decays, cosmology (BBN, CMB, LSS), dedicated searches.

# Conclusions

- Neutrino oscillations imply that neutrinos have mass and mix: First particle physics evidence of physics beyond the SM. They provide a complementary window w.r.t. collider and flavour physics searches.



- The ultimate goal is to understand the origin of neutrino masses and leptonic mixing.
- It is necessary to know the values of the masses and of the mixing angles and CPV phase (with precision!). An exciting experimental programme is under way.